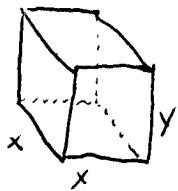


Math 16A: Short Calculus I
 Fall 2017, Section 3
 Homework Sheet 8
 Due: Monday, November 27, 2017

Submit your solutions to the following problems in lecture on the due date above. Present your work in a clean and organized fashion, either on a printed copy of this document (preferred) or a separate sheet of paper. As stated in the syllabus, late submissions will **not** be accepted.

1. Suppose you want to build a jewelry box with a square bottom and open top. If you have 12 ft² of building material, what are the dimensions of the box with the maximum volume?



$x = \text{width}$ $A = \text{surface area} = 12$
 $y = \text{height}$ $V = \text{volume}$

$$12 = x^2 + 4xy$$

$$12 - x^2 = 4xy$$

$$y = \frac{12 - x^2}{4x}$$

$$V = x^2 y$$

$$V = x^2 \left(\frac{12 - x^2}{4x} \right)$$

$$V = \frac{3}{4}x - \frac{1}{4}x^3$$

$$V'(x) = \frac{3}{4} - \frac{3}{4}x^2 = 0$$

$$\frac{3}{4} = \frac{3}{4}x^2$$

$$y = x^2$$

$$x = 2, \quad x = -2$$

plug in crit #s
and endpoints:

$$V(2) = 6 - 2 = 4$$

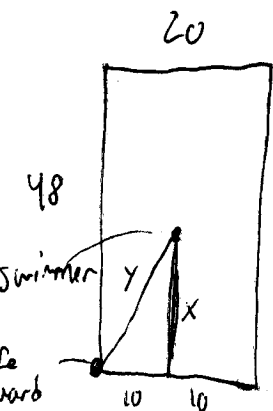
$$V(0) = 0$$

$$V(-\sqrt{12}) = 3\sqrt{12} - \frac{1}{4}(\sqrt{12})^3 = 0$$

when $x = \sqrt{12}$,
bottom of box
has area 12 ft²,
so all material used.

dimensions:
 $x = 2$
 $y = \frac{12 - 4}{8} = 1$

2. Suppose you are swimming 20 ft/sec in a 20ft by 48ft pool, long-ways in the middle lane (i.e. 10 ft from each of the longer sides). There is a lifeguard standing at the corner of the pool, watching you swim away. How fast is your distance from the lifeguard changing when you are halfway across the pool?



$x = \text{dist swimmer to wall}$
 $y = \text{dist swimmer to lifeguard}$

$$10^2 + (x(t))^2 = (y(t))^2$$

$$0 + 2x(t) \frac{dx}{dt} = 2y(t) \frac{dy}{dt}$$

$$2(24)(20) = 2(26) \frac{dy}{dt}$$

$$\frac{dy}{dt} = \frac{2(24)(20)}{2(26)} \text{ ft/sec}$$

halfway across pool:

$$x = 24$$

$$10^2 + 24^2 = y^2$$

$$y = 26$$