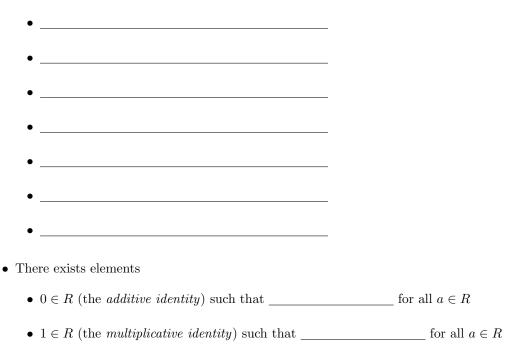
Fall 2021, Math 620: Preliminary Problem Set 6 Due: Thursday, September 30th, 2021 Introduction To Rings

Preliminary problems. These problems should be completed before discussion on Thursday.

- (P1) Listed below are the axioms for $(R, +, \cdot)$ to be a field. Fill in the blanks.
 - For every $a, b, c \in R$,



- For each $a \in R$,
 - there is an element $b \in R$ (the *additive inverse* of *a*) with $a + b = ___= 0$
 - if $a \neq _$, there exists $b \in R$ (the multiplicative inverse of a) with $ab = ba = _$
- (P2) Write "(I)" next to each item above that is needed to ensure (F, +) is an integral domain. Note: this requires adding an additional axiom at the end!
- (P3) Write "(R)" next to each axiom item that is needed to ensure $(F, +, \cdot)$ is a ring.