Fall 2021, Math 620: Preliminary Problem Set 6 Due: Thursday, September 30th, 2021

Introduction To Rings

Preliminary problems. These problems should be completed before discussion on Thursday.
(P1) Listed below are the axioms for $(R,+, \cdot)$ to be a field. Fill in the blanks.

- For every $a, b, c \in R$,
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$\qquad$
$\bullet$
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$\bullet$ $\qquad$
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- 
- There exists elements
- $0 \in R$ (the additive identity) such that $\qquad$ for all $a \in R$
- $1 \in R$ (the multiplicative identity) such that $\qquad$ for all $a \in R$
- For each $a \in R$,
- there is an element $b \in R$ (the additive inverse of $a$ ) with $a+b=$ $\qquad$ $=0$
- if $a \neq \ldots$, there exists $b \in R$ (the multiplicative inverse of $a$ ) with $a b=b a=$ $\qquad$
(P2) Write "(I)" next to each item above that is needed to ensure $(F,+)$ is an integral domain. Note: this requires adding an additional axiom at the end!
(P3) Write "(R)" next to each axiom item that is needed to ensure $(F,+, \cdot)$ is a ring.

