

Fall 2022, Math 522: Preliminary Problem Set 4
Due: Wednesday, September 21st, 2022
Modular Arithmetic

Preliminary problems. These problems should be completed before discussion.

(P1) Fill in the addition and multiplication tables for \mathbb{Z}_6 below. **For this problem**, you may omit the $[\]_6$ notation to save time/space.

| + | $[0]_6$ | $[1]_6$ | $[2]_6$ | $[3]_6$ | $[4]_6$ | $[5]_6$ |
|---------|---------|---------|---------|---------|---------|---------|
| $[0]_6$ | 0 | | | | | |
| $[1]_6$ | | | | | | |
| $[2]_6$ | | | | 5 | | |
| $[3]_6$ | | | | | | |
| $[4]_6$ | | | | 1 | | |
| $[5]_6$ | | | | | | |

| · | $[0]_6$ | $[1]_6$ | $[2]_6$ | $[3]_6$ | $[4]_6$ | $[5]_6$ |
|---------|---------|---------|---------|---------|---------|---------|
| $[0]_6$ | | | 0 | | | |
| $[1]_6$ | | | | | | |
| $[2]_6$ | | | | | 2 | |
| $[3]_6$ | | | | | | |
| $[4]_6$ | | | | | | |
| $[5]_6$ | | | | | | 1 |

(P2) Find all $x \in \mathbb{Z}_7$ that satisfy $x^2 = [4]_7$.

(P3) In the previous problem, is x an integer or an equivalence class? Be sure your answer above reflects this!