Fall 2023, Math 320: Preliminary Problem Set 3

## Due: Thursday, September 14th, 2023

Modular Arithmetic

Preliminary problems. These problems should be completed before discussion on Thursday.
(P1) Fill in the addition and multiplication tables for $\mathbb{Z}_{6}$ below. For this problem, you may omit the []$_{6}$ notation to save time/space.

| + | $[0]_{6}$ | $[1]_{6}$ | $[2]_{6}$ | $[3]_{6}$ | $[4]_{6}$ | $[5]_{6}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $[0]_{6}$ | 0 |  |  |  |  |  |
| $[1]_{6}$ |  |  |  |  |  |  |
| $[2]_{6}$ |  |  |  | 5 |  |  |
| $[3]_{6}$ |  |  |  |  |  |  |
| $[4]_{6}$ |  |  |  | 1 |  |  |
| $[5]_{6}$ |  |  |  |  |  |  |


| $\cdot$ | $[0]_{6}$ | $[1]_{6}$ | $[2]_{6}$ | $[3]_{6}$ | $[4]_{6}$ | $[5]_{6}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $[0]_{6}$ |  |  | 0 |  |  |  |
| $[1]_{6}$ |  |  |  |  |  |  |
| $[2]_{6}$ |  |  |  |  | 2 |  |
| $[3]_{6}$ |  |  |  |  |  |  |
| $[4]_{6}$ |  |  |  |  |  |  |
| $[5]_{6}$ |  |  |  |  |  | 1 |

(P2) Find all $x \in \mathbb{Z}_{7}$ that satisfy $x^{2}=[4]_{7}$.
(P3) In the previous problem, is $x$ an integer or an equivalence class? Be sure your answer above reflects this!

