Fall 2023, Math 320: Preliminary Problem Set 6
Due: Thursday, October 5th, 2023
Arithmetic in Rings

Preliminary problems. These problems should be completed before discussion on Thursday.

(P1) Fill in the blanks in the following axioms from the definition of a ring $(R, +, \cdot)$. Be sure to include all relevant quantifiers (for all, there exists).

(a) Multiplication in R is associative, that is, _____,

$$a(bc) = (ab)c.$$

(b) The ring R has an additive identity, that is, _____ such that

$$0_R + a = a + 0_R = a$$

for all $a \in R$.

(c) Every element of R has an additive inverse in R, that is, _____, there exists $(-a) \in R$ such that

_____.