

**Spring 2019, Math 320: Preliminary Problem Set 3**  
**Due: Thursday, February 14th, 2019**  
**Modular Arithmetic**

**Preliminary problems.** These problems should be completed before discussion on Thursday.

(P1) Fill in the addition and multiplication tables for  $\mathbb{Z}_6$  below. You may omit the  $[\ ]_6$  notation if you prefer.

| +       | $[0]_6$ | $[1]_6$ | $[2]_6$ | $[3]_6$ | $[4]_6$ | $[5]_6$ |
|---------|---------|---------|---------|---------|---------|---------|
| $[0]_6$ | 0       |         |         |         |         |         |
| $[1]_6$ |         |         |         |         |         |         |
| $[2]_6$ |         |         |         | 5       |         |         |
| $[3]_6$ |         |         |         |         |         |         |
| $[4]_6$ |         |         |         |         |         |         |
| $[5]_6$ |         |         |         |         |         |         |

| ·       | $[0]_6$ | $[1]_6$ | $[2]_6$ | $[3]_6$ | $[4]_6$ | $[5]_6$ |
|---------|---------|---------|---------|---------|---------|---------|
| $[0]_6$ |         |         | 0       |         |         |         |
| $[1]_6$ |         |         |         |         |         |         |
| $[2]_6$ |         |         |         |         |         |         |
| $[3]_6$ |         |         |         |         |         |         |
| $[4]_6$ |         |         |         |         |         |         |
| $[5]_6$ |         |         |         |         |         | 1       |

(P2) Find all  $x \in \mathbb{Z}_7$  that satisfy  $x^2 = [4]_7$ .