Preliminary problems. These problems should be completed before discussion on Thursday.
(P1) Find a rational expression for the $\operatorname{Hilbert} \operatorname{series} \operatorname{Hilb}(R ; z)$ of each of the following rings $R$.
(a) $R=\mathbb{k}[x, y]$ with $\operatorname{deg}(x)=\operatorname{deg}(y)=2$.
(b) $R=\mathbb{k}[x, y] /\langle x y\rangle$ with $\operatorname{deg}(x)=\operatorname{deg}(y)=2$.

