## Math 621: Algebraic Topology Spring 2021

Instructor:Christopher O'NeillOffice:Room 570, Geology Mathematics and Computer Science (GMCS) BuildingE-mail:cdoneill@sdsu.eduWebpage:http://cdoneill.sdsu.edu/teaching/s21-621

**Course Content:** Algebraic invariants of topological spaces. Simplicial and cellular complexes, homotopy equivalence, the fundamental group, covering spaces, and homology. Additional topics as time permits.

Texts: Content will be sampled from the following textbooks. All are optional, but will be useful references.

- Algebraic Topology, by Allen Hatcher.
- Elements of Algebraic Topology, by James Munkres.

**Prerequisites:** Math 620 with a grade of C or better.

Course Organization: The class will be organized as follows.

- One class day each week (usually Tuesday), I will give a lecture on course material (a "lecture day").
- The other day each week (usually Thursday), you will work in small groups (a "discussion day").

A problem list will be distributed at the beginning of each discussion day containing both the in-class work problems (which **will introduce new material**) and the weekly homework problems. All completed homework problems will be turned in for credit, usually the following Thursday.

The day before each discussion day, a short list of "preliminary problems" will be assigned, and should be completed before class on the discussion day. These assignments will be short, usually requiring at most 10 minutes to complete, and will be computational in nature (i.e. no proofs).

Although I intend to use this format throughout the course, I reserve the right to restructure the course as the term progresses, based in part on student feedback and performance. I will periodically collect anonymous feedback in class, but feel free to come talk to me if you have suggestions or concerns.

**Grading Policy:** Your grade will be determined by weekly homework sets, a participation grade, and a project, weighted as follows.

Homework	60%	A = 90-100
Project	30%	B = 80-89
Participation	10%	C = 70-79
Total	100%	D = 60-69
		F = 0.59

Although there is no final exam, our final exam period, scheduled for Thursday, May 13th from 10:30am-12:30pm, will be utilized for project presentations. Keep this date in mind when making travel plans for the end of the term.

**Participation:** Attendance in discussion days is vital to success in this class, since **new material** will be covered. Your participation grade will be based on the following:

- attending and participating in lectures;
- attending and engaging in discussion days; and
- completing the preliminary problems before each discussion day.

Missing class will result in a lowered participation grade, and only university excused absences with **advance notice** to the instructor will be accepted. I reserve the right to deduct one **additional full letter grade** if you miss too many classes, or if sufficient participation is not demonstrated during discussion days.

Homework: There will be one homework assignment given each week, as well as a short list of preliminary problems to be completed before each problem session. Completed homework assignments **must be typeset in \underline{LATE}X** and will be submitted to the instructor for a grade; preliminary problems will not be collected. Collaboration on homework is encouraged, but solutions should be written individually, and **collaborators should be identified** on the front of your assignment.

Homework assignments, along with their due dates, will be posted on the course webpage as they are assigned. Out of fairness to the other students, late homework assignments will not be accepted for credit. However, the lowest homework grade of the term will be dropped.

**Project:** Each student will complete an independent project. Topics can be selected from a list provided by the instructor, or chosen independently, but must be approved either way. The project grade will be determined by

- regular progress in meetings with the instructor,
- a final writeup due on the final exam day, and
- a final presentation during the final exam time.

**Class Announcements, E-mail Policy and Communications:** Class announcements will be posted to my class web page and sent to your university e-mail account. Be sure to regularly check your e-mail. If you send me an e-mail, please include your name and course information (i.e. class and section) as well as any additional information that I might need to respond to your e-mail.

## Attendance, Absence, and Makeup Work Policies:

- Attendance is essential for success in the course, especially discussion days!
- Late homework will not be accepted. However, your lowest homework grade will be dropped.
- The last day to drop this class is February 2nd.

## **Student Learning Outcomes:**

- Students will be able to write clear, correct proofs of mathematical statements involving topological spaces.
- Students will be able to use homological algebraic methods, including long exact sequences, excision and Mayer-Veitorus, to compute homology of cell complexes.
- Students will be able to solve open-ended problems involving algebraic and topological objects by first formulating conjectures from examples and topological intution, and then proving their conjectures using rigorous mathematical arguments.
- Students will be able to work together to collaboratively solve difficult mathematics problems.

**A.D.A. Policy Statement:** The Americans with Disabilities Act (ADA) is a federal anti-discrimination statute that provides comprehensive civil rights protection for persons with disabilities. This legislation requires that all students with disabilities be guaranteed a learning environment that provides for reasonable accommodation of their disabilities. If you believe you have a disability requiring accommodation, please contact Student Disability Services.

If you require additional time on quizzes and/or exams, you must **contact me at the start of the course**. You will not be given extra time if you present this information just before an exam.

For additional information, visit https://go.sdsu.edu/student\_affairs/sds/.

**Copyright Policy:** The handouts used in this course are copyrighted. By "handouts," I mean all materials generated for this class, which include but are not limited to syllabi, quizzes, exams, in-class materials, review sheets, and additional problems sets. Because these materials are copyrighted, you do not have the right to copy the handouts, unless I expressly grant permission.

**Scholastic Dishonesty:** <u>An Aztec Does Not Lie, Cheat, or Steal, or Tolerate Those Who Do.</u> The San Diego State University Student Conduct Code will be enforced in this course. For the purpose of this course, cheating will be defined as (but not limited to) access or use of unauthorized material during exams and quizzes, collaboration between students during exams, quizzes or assignments for which group work is not allowed, perusal of another student's work during exams and quizzes, copying other student's work or allowing other students to copy your work on any assignment, quiz or exam, and having unauthorized programs or other information stored on calculators when these calculators are accessible during an exam or quiz. Note: Falsifying documentation is considered scholastic dishonesty and may result in a grade of F for the course.</u>

For additional information, visit http://go.sdsu.edu/student\_affairs/srr/conduct.aspx.