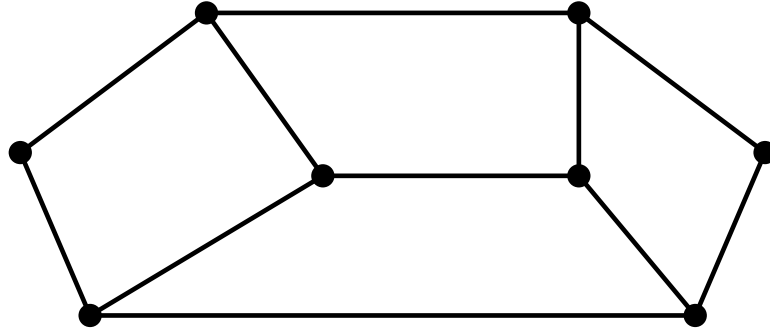


Spring 2024, Math 579: Preliminary Problem Set 12
Due: Thursday, April 18th, 2024
Colorings and Bipartite Graphs

Preliminary problems. These problems should be completed before discussion on Thursday.

- (P1) Find a 2-coloring of the graph depicted below. Redraw the graph with vertices of one color on the left and the remaining vertices on the right (how we usually draw bipartite graphs).



- (P2) Consider the cycle graph C_4 with the vertices labeled 1, 2, 3, 4 clockwise. Find the number of ways to properly color C_4 using the colors red, green, and blue. How many of the colorings use **exactly** those 3 colors (that is, every color appears at least once)?