

Spring 2026, Math 590: Week 7 Preliminary Problems
Due: Wednesday, March 18th, 2026
Faces of Polyhedra

Preliminary problems. These problems should be completed before discussion on Wednesday.

(P1) Draw the polytope

$$P = \text{conv}\{(0, 0, 0), (1, 0, 0), (0, 1, 0), (1, 1, 0), (0, 0, 1)\} \subset \mathbb{R}^3.$$

(P2) Write down an inequality $a_1x_1 + a_2x_2 + a_3x_3 \leq b$ that defines a half-space demonstrating \emptyset is a face of P .

(P3) Write down an inequality $a_1x_1 + a_2x_2 + a_3x_3 \leq b$ that defines a half-space demonstrating P is a face of P .

(P4) Let

$$v_1 = (0, 0, 0), \quad v_2 = (1, 0, 0), \quad v_3 = (0, 1, 0), \quad v_4 = (1, 1, 0), \quad \text{and} \quad v_5 = (0, 0, 1).$$

Write down each subset of the vertices of P whose convex hull is a face of P . To conserve space/ink/sanity, omit commas, curly-braces, and v 's, writing e.g., 124 for $\{v_1, v_2, v_4\}$.

Note: there are 20 faces total.