

**Winter 2017, Math 148: Week 4 Preliminary Problems**  
**Due: Thursday, February 2nd, 2017**  
**Finite Fields**

**Preliminary problems.** These problems should be completed before discussion on Thursday.

(P1) Let  $\mathbb{F}_4 = \mathbb{Z}_2[z]/\langle z^2 + z + 1 \rangle$  as in Wednesday's class. Fill in the addition and multiplication tables for  $\mathbb{F}_4$ , and verify that they coincide with those you found in discussion on Monday.

(P2) Find all irreducible polynomials in  $\mathbb{Z}_2[z]$  of degree at most 3.