

Math 16B: Short Calculus II
 Winter 2018, Section 3
 Homework Sheet 5
 Due: Friday, February 23, 2018

Submit your solutions to the following problems in lecture on the due date above. Present your work in a clean and organized fashion, either on a printed copy of this document (preferred) or a separate sheet of paper. As stated in the syllabus, late submissions will **not** be accepted.

1. Evaluate the following integrals using U-substitution.

(a) $\int \cos(x)e^{\sin(x)} dx$

let $u = \sin(x)$
 $\frac{du}{dx} = \cos(x)$
 $du = \cos(x) dx$

$$\int e^u du = e^u + C$$

$$= \boxed{e^{\sin(x)} + C}$$

(b) $\int x^2 \sin(x^3 + 3) dx$

let $u = x^3 + 3$
 $\frac{du}{dx} = 3x^2$
 $\frac{1}{3} du = x^2 dx$

$$\int \frac{1}{3} \sin(u) du = -\frac{1}{3} \cos(u) + C$$

$$= \boxed{-\frac{1}{3} \cos(x^3 + 3) + C}$$

(c) $\int \frac{x^2 + 3}{\sqrt[3]{x^3 + 9x}} dx$

let $u = x^3 + 9x$
 $\frac{du}{dx} = 3x^2 + 9$
 $\frac{1}{3} du = (x^2 + 3) dx$

$$\int \frac{1/3}{u^{1/3}} du = \frac{1}{3} \cdot \frac{3}{2} u^{2/3} + C$$

$$= \boxed{\frac{1}{2} (x^3 + 9x)^{2/3} + C}$$

(d) $\int_{\pi/4}^{\pi/2} \cot(x) dx$

let $u = \sin(x)$
 $\frac{du}{dx} = \cos(x)$
 $du = \cos(x) dx$

$$\int_{x=\pi/4}^{x=\pi/2} \frac{\cos(x)}{\sin(x)} dx = \int_{u=\pi/4}^{u=\pi/2} \frac{1}{u} du = \ln|u| \Big|_{x=\pi/4}^{x=\pi/2}$$

$$= \ln|\sin(x)| \Big|_{x=\pi/4}^{x=\pi/2}$$

$$= \boxed{\ln\left|\sin\left(\frac{\pi}{2}\right)\right| - \ln\left|\sin\left(\frac{\pi}{4}\right)\right|}$$